

Typeclasses

Announcements

- HW 04-NANO – deadline ==> May 31, 23:59:59

```
``haskell let fac = – env0 -> if n <= 0 then 1 else 1 * fac (n-1) in fac 5
```

let f = e1 in e2 ...

– Somehow “hack the frozen env” so that the name f – is “available” in the closure’s frozen env that e1 – evaluates to

VClos env0 “n” <if n <=0 ... >

eval (("n", 5):env0) <body>

PROBLEM: ‘fac’ is unbound in env0 and hence in ("n", 5) : env0

Past two Weeks

How to *implement* language constructs?

- Local variables and scope

- Environments and Closures

Next two Weeks

Modern language features for structuring programs

- Type classes
- Monads

Overloading Operators: Arithmetic

The + operator works for a bunch of different types.

For Integer :

```
λ> 2 + 3
```

```
5
```

for Double precision floats:

```
λ> 2.9 + 3.5
```

```
6.4
```

Overloading Comparisons

Similarly we can *compare* different types of values

```
λ> 2 == 3
```

```
False
```

```
λ> [2.9, 3.5] == [2.9, 3.5]
```

```
True
```

```
λ> ("cat", 10) < ("cat", 2)
```

```
False
```

```
λ> ("cat", 10) < ("cat", 20)
```

```
True
```

Ad-Hoc Overloading

Seems unremarkable?

Languages since the dawn of time have supported “operator overloading”

- To support this kind of **ad-hoc polymorphism**

- Ad-hoc: “created or done for a particular purpose as necessary.”

You really **need** to *add* and *compare* values of *multiple* types!

Haskell has no caste system

No distinction between operators and functions

- All are first class citizens!

But then, what type do we give to *functions* like `+` and `==` ?

QUIZ

Which of the following would be appropriate types for `(+)` ?

(A) $(+) :: \text{Integer} \rightarrow \text{Integer} \rightarrow \text{Integer}$

(B) $(+) :: \text{Double} \rightarrow \text{Double} \rightarrow \text{Double}$

(C) $(+) :: a \rightarrow a \rightarrow a$

(D) *All of the above*

(E) *None of the above*

$\text{Integer} \rightarrow \text{Integer} \rightarrow \text{Integer}$ is bad because?

- Then we cannot add `Double` s!

Double -> Double -> Double is bad because?

- Then we cannot add Double s!

a -> a -> a is bad because?

- That doesn't make sense, e.g. to add two Bool or two [Int] or two functions!

Type Classes for Ad Hoc Polymorphism

Haskell solves this problem with an *insanely slick* mechanism called typeclasses, introduced by Wadler and Blott (<http://portal.acm.org/citation.cfm?id=75283>)

How to make *ad-hoc* polymorphism less *ad hoc*

Philip Wadler and Stephen Blott
University of Glasgow*

October 1988

BTW: The paper is one of the clearest examples of academic writing I have seen. The next time you hear a curmudgeon say all the best CS was done in the 60s, just point them to the above.

Qualified Types

To see the right type, lets ask:

```
λ> :type (+)
```

```
(+) :: (Num a) => a -> a -> a
```

We call the above a **qualified type**. Read it as +

- takes in two `a` values and returns an `a` value

for any type `a` that

- *is a* `Num` or
- *implements* the `Num` interface or
- *is an instance of* a `Num`.

The name `Num` can be thought of as a *predicate* or *constraint* over types.

Some types are *Nums*

Examples include `Integer`, `Double` etc

- Any such values of those types can be passed to `+`.

Other types are not `Num`s

Examples include `Char`, `String`, functions etc,

- Values of those types *cannot* be passed to `+`.

```
λ> True + False
```

```
<interactive>:15:6:
```

```
  No instance for (Num Bool) arising from a use of '+'
```

```
  In the expression: True + False
```

```
  In an equation for 'it': it = True + False
```

Aha! Now those no **instance** for error messages should make sense!

- Haskell is complaining that `True` and `False` are of type `Bool`
- and that `Bool` is *not* an instance of `Num`.

Type Class is a Set of Operations

A typeclass is a collection of operations (functions) that must exist for the underlying type.

The *Eq* Type Class

The simplest typeclass is perhaps, Eq

```
class Eq a where  
  (==) :: a -> a -> Bool  
  (/=) :: a -> a -> Bool
```

A type `a` is an instance of Eq if there are two functions

- == and /=

That determine if two `a` values are respectively *equal* or *disequal*.

The *Show* Type Class

The typeclass Show requires that instances be convertible to String (which can then be printed out)

```
class Show a where  
  show :: a -> String
```

Indeed, we can test this on different (built-in) types

```
λ> show 2
```

```
"2"
```

```
λ> show 3.14
```

```
"3.14"
```

```
λ> show (1, "two", ([],[],[]))
```

```
"(1,\"two\",([],[],[]))"
```

(Hey, whats up with the funny \" ?)

When we type an expression into ghci, it computes the value and then calls `show` on the result. Thus, if we create a *new* type by

```
data Unshowable = A | B | C
```

and then create values of the type,

```
λ> let x = A
```

```
λ> :type x
```

```
x :: Unshowable
```

but then we **cannot view** them

```
λ> x
```

```
<interactive>:1:0:
```

```
No instance for (Show Unshowable)
```

```
arising from a use of `print' at <interactive>:1:0
```

```
Possible fix: add an instance declaration for (Show Unshowable)
```

```
In a stmt of a 'do' expression: print it
```

and we **cannot compare** them!

```
λ> x == x
```

```
<interactive>:1:0:
```

```
No instance for (Eq Unshowable)
```

```
arising from a use of `==' at <interactive>:1:0-5
```

```
Possible fix: add an instance declaration for (Eq Unshowable)
```

```
In the expression: x == x
```

```
In the definition of `it': it = x == x
```

Again, the previously incomprehensible type error message should make sense to you.

Creating Instances

Tell Haskell how to show or compare values of type Unshowable

By **creating instances** of Eq and Show for that type:

instance Eq Unshowable **where**

```
(==) A A = True           -- True if both inputs are A
(==) B B = True           -- ...or B
(==) C C = True           -- .. or C
(==) _ _ = False         -- otherwise

(/=) x y = not (x == y)  -- Test if `x == y` and negate result!
```

EXERCISE Lets create an **instance** for Show Unshowable

Automatic Derivation

This is silly: we *should* be able to compare and view Unshowable “automatically”!

Haskell lets us *automatically derive* functions for some classes in the standard library.

To do so, we simply dress up the data type definition with

```
data Showable = A' | B' | C'
  deriving (Eq, Show) -- tells Haskell to automatically generate instances
```

Now we have

```
λ> let x' = A'
```

```
λ> :type x'
```

```
x' :: Showable
```

```
λ> x'
```

```
A'
```

```
λ> x' == x'
```

```
True
```

```
λ> x' == B'
```

```
False
```

Standard Typeclass Hierarchy

Let us now peruse the definition of the Num typeclass.

```
λ> :info Num
```

```
class (Eq a, Show a) => Num a where
```

```
  (+) :: a -> a -> a
```

```
  (*) :: a -> a -> a
```

```
  (-) :: a -> a -> a
```

```
  negate :: a -> a
```

```
  abs :: a -> a
```

```
  signum :: a -> a
```

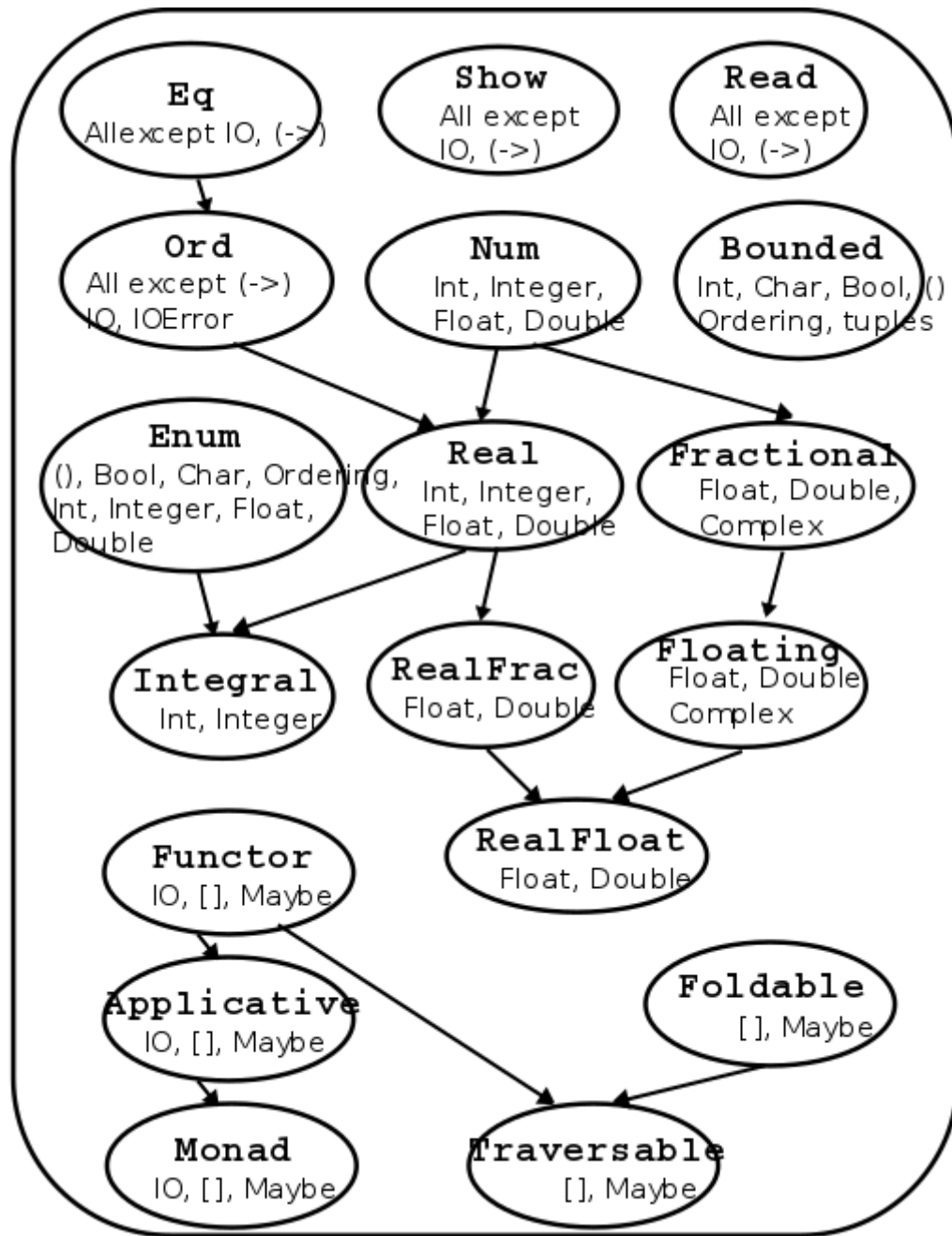
```
  fromInteger :: Integer -> a
```

A type `a` is an instance of (i.e. implements) `Num` if

1. The type is *also* an instance of `Eq` and `Show`, and
2. There are functions for adding, multiplying, subtracting, negating etc values of that type.

In other words in addition to the “arithmetic” operations, we can compare two `Num` values and we can view them (as a `String`.)

Haskell comes equipped with a rich set of built-in classes.



Standard Typeclass Hierarchy

In the above picture, there is an edge from Eq and Show to Num because for something to be a Num it must also be an Eq and Show.

The Ord Typeclass

Another typeclass you've used already is the one for Ordering values:

```
λ> :info (<)  
class Eq a => Ord a where  
  ...  
  (<) :: a -> a -> Bool  
  ...
```

For example:

```
λ> 2 < 3  
True
```

```
λ> "cat" < "dog"  
True
```

QUIZ

Recall the datatype:

```
data Showable = A' | B' | C' deriving (Eq, Show)
```

What is the result of:

$\lambda > A' < B'$

(A) True (B) False (C) Type error (D) Run-time exception

Using Typeclasses

Typeclasses integrate with the rest of Haskell's type system.

Lets build a small library for *Environments* mapping keys k to values v

```
data Env k v
  = Def v -- default value `v` to be used for "missing" keys
  | Bind k v (Env k v) -- bind key `k` to the value `v`
deriving (Show)
```

An API for Env

Lets write a small API for Env

```
-- >>> let env0 = add "cat" 10.0 (add "dog" 20.0 (Def 0))
```

```
-- >>> get "cat" env0
```

```
-- 10
```

```
-- >>> get "dog" env0
```

```
-- 20
```

```
-- >>> get "horse" env0
```

```
-- 0
```

Ok, lets implement!

```
-- | 'add key val env' returns a new env that additionally maps `key` to `val`
```

```
add :: k -> v -> Env k v -> Env k v
```

```
add key val env = ???
```

```
-- | 'get key env' returns the value of `key` and the "default" if no value is found
```

```
get :: k -> Env k v -> v
```

```
get key env = ???
```

Oops, y u no check?

Constraint Propagation

Lets *delete* the types of `add` and `get` and see what Haskell says their types are!

```
λ> :type get
get :: (Eq k) => k -> v -> Env k v -> Env k v
```

Haskell tells us that we can use any `k` value as a *key* as long as the value is an instance of the `Eq` typeclass.

How, did GHC figure this out?

- If you look at the code for `get` you'll see that we check if two keys *are equal!*

Exercise

Write an optimized version of

- `add` that ensures the keys are in *increasing* order,
- `get` that gives up and returns the “default” the moment we see a key that's larger than the one we're looking for.

(How) do you need to change the type of `Env`?

(How) do you need to change the types of `get` and `add`?

Explicit Signatures

While Haskell is pretty good about inferring types in general, there are cases when the use of type classes requires explicit annotations (which change the behavior of the code.)

For example, `Read` is a built-in typeclass, where any instance `a` of `Read` has a function

```
read :: (Read a) => String -> a
```

which can parse a string and turn it into an `a`.

That is, `Read` is the *opposite* of `Show`.

Quiz

What does the expression `read "2"` evaluate to?

- (A) compile time error
- (B) `"2" :: String`
- (C) `2 :: Integer`
- (D) `2.0 :: Double`
- (E) run-time exception

Haskell is foxed!

- Doesn't know *what type* to convert the string to!
- Doesn't know *which* of the `read` functions to run!

Did we want an `Int` or a `Double` or maybe something else altogether?

Thus, here an **explicit type annotation** is needed to tell Haskell what to convert the string to:

```
λ> (read "2") :: Int  
2
```

```
λ> (read "2") :: Float  
2.0
```

Note the different results due to the different types.

Creating Typeclasses

Typeclasses are useful for *many* different things.

We will see some of those over the next few lectures.

Lets conclude today's class with a quick example that provides a small taste.

JSON

JavaScript Object Notation or JSON (<http://www.json.org/>) is a simple format for transferring data around. Here is an example:

```
{ "name"      : "Ranjit"
  , "age"      : 41.0
  , "likes"    : ["guacamole", "coffee", "bacon"]
  , "hates"    : [ "waiting" , "grapefruit"]
  , "lunches" : [ {"day" : "monday",   "loc" : "zanzibar"}
                  , {"day" : "tuesday", "loc" : "farmers market"}
                  , {"day" : "wednesday", "loc" : "harekrishna"}
                  , {"day" : "thursday", "loc" : "faculty club"}
                  , {"day" : "friday",   "loc" : "coffee cart"} ]
}
```

In brief, each JSON object is either

- a *base* value like a string, a number or a boolean,
- an (ordered) *array* of objects, or
- a set of *string-object* pairs.

A JSON Datatype

We can represent (a subset of) JSON values with the Haskell datatype


```
data JVal
  = JStr  String
  | JNum  Double
  | JBool Bool
  | JObj  [(String, JVal)]
  | JArr  [JVal]
deriving (Eq, Ord, Show)
```

Thus, the above JSON value would be represented by the JVal

```
js1 =
  JObject [("name", JStr "Ranjit")
    ,("age", JNum 41.0)
    ,("likes", JArr [ JStr "guacamole", JStr "coffee", JStr "bacon" ])
    ,("hates", JArr [ JStr "waiting" , JStr "grapefruit" ])
    ,("lunches", JArr [ JObject [("day", JStr "monday")
      ,("loc", JStr "zanzibar" )]
      , JObject [("day", JStr "tuesday")
      ,("loc", JStr "farmers market" )]
      , JObject [("day", JStr "wednesday")
      ,("loc", JStr "hare krishna" )]
      , JObject [("day", JStr "thursday")
      ,("loc", JStr "faculty club" )]
      , JObject [("day", JStr "friday")
      ,("loc", JStr "coffee cart" )]
    ])
  ]
```

Serializing Haskell Values to JSON

Lets write a small library to *serialize* Haskell values as JSON.

We could write a bunch of functions like

```
doubleToJSON :: Double -> JVal
doubleToJSON = JNum
```

```
stringToJSON :: String -> JVal
stringToJSON = JStr
```

```
boolToJSON    :: Bool -> JVal
boolToJSON    = JBool
```

Serializing Collections

But what about collections, namely *lists* of things?

```
doublesToJSON    :: [Double] -> JVal
doublesToJSON xs = JArr (map doubleToJSON xs)
```

```
boolsToJSON      :: [Bool] -> JVal
boolsToJSON xs   = JArr (map boolToJSON xs)
```

```
stringsToJSON    :: [String] -> JVal
stringsToJSON xs = JArr (map stringToJSON xs)
```

This is **getting rather tedious**

- We are rewriting the same code :(

Serializing Collections (refactored with HOFs)

You could abstract by making the *individual-element-converter* a parameter

```
xstoJSON :: (a -> JVal) -> [a] -> JVal
```

```
xstoJSON f xs = JArr (map f xs)
```

```
xysToJSON :: (a -> JVal) -> [(String, a)] -> JVal
```

```
xysToJSON f kvs = JObject [ (k, f v) | (k, v) <- kvs ]
```

But this is **still rather tedious** as you have to pass in the individual data converter (yuck)

```
λ> doubleToJSON 4
```

```
JNum 4.0
```

```
λ> xsToJSON stringToJSON ["coffee", "guacamole", "bacon"]
```

```
JArr [JStr "coffee",JStr "guacamole",JStr "bacon"]
```

```
λ> xysToJSON stringToJSON [("day", "monday"), ("loc", "zanzibar")]
```

```
JObj [("day",JStr "monday"),("loc",JStr "zanzibar")]
```

This gets more hideous when you have richer objects like

```
lunches = [ [("day", "monday"),    ("loc", "zanzibar")]
            , [("day", "tuesday"), ("loc", "farmers market")]
            ]
```

because we have to go through gymnastics like

```
λ> xsToJSON (xysToJSON stringToJSON) lunches
```

```
JArr [ JObj [("day",JStr "monday")    ,("loc",JStr "zanzibar")]
```

```
      , JObj [("day",JStr "tuesday")  ,("loc",JStr "farmers market")]
```

```
      ]
```

Yikes. So much for *readability*

Is it too much to ask for a magical `toJSON` that *just works*?

Typeclasses To The Rescue

Lets *define* a typeclass that describes types `a` that can be converted to JSON.

```
class JSON a where  
  toJSON :: a -> JVal
```

Now, just make all the above instances of `JSON` like so

```
instance JSON Double where  
  toJSON = JNum
```

```
instance JSON Bool where  
  toJSON = JBool
```

```
instance JSON String where  
  toJSON = JStr
```

This lets us uniformly write

```
λ> toJSON 4
```

```
JNum 4.0
```

```
λ> toJSON True
```

```
JBool True
```

```
λ> toJSON "guacamole"
```

```
JStr "guacamole"
```

Bootstrapping Instances

The real fun begins when we get Haskell to automatically bootstrap the above functions to work for lists and key-value lists!

```
instance JSON a => JSON [a] where
```

```
  toJSON xs = JArr [toJSON x | x <- xs]
```

The above says, if `a` is an instance of `JSON`, that is, if you can convert `a` to `JVal` then here's a generic recipe to convert lists of `a` values!

```
λ> toJSON [True, False, True]
```

```
JArr [JBln True, JBln False, JBln True]
```

```
λ> toJSON ["cat", "dog", "Mouse"]
```

```
JArr [JStr "cat", JStr "dog", JStr "Mouse"]
```

or even lists-of-lists!

```
λ> toJSON ["cat", "dog"], ["mouse", "rabbit"]  
JArr [JArr [JStr "cat",JStr "dog"],JArr [JStr "mouse",JStr "rabbit"]]
```

We can pull the same trick with key-value lists

```
instance (JSON a) => JSON [(String, a)] where  
  toJSON kvs = JObject [ (k, toJSON v) | (k, v) <- kvs ]
```

after which, we are all set!

```
λ> toJSON lunches  
JArr [ JObject [ ("day",JStr "monday"), ("loc",JStr "zanzibar") ]  
      , JObject [ ("day",JStr "tuesday"), ("loc",JStr "farmers market") ]  
      ]
```

It is also useful to bootstrap the serialization for tuples (upto some fixed size) so we can easily write “non-uniform” JSON objects where keys are bound to values with different shapes.


```

instance (JSON a, JSON b) => JSON ((String, a), (String, b)) where
  toJSON ((k1, v1), (k2, v2)) =
    JObj [(k1, toJSON v1), (k2, toJSON v2)]

instance (JSON a, JSON b, JSON c) => JSON ((String, a), (String, b), (String, c)) where
  toJSON ((k1, v1), (k2, v2), (k3, v3)) =
    JObj [(k1, toJSON v1), (k2, toJSON v2), (k3, toJSON v3)]

instance (JSON a, JSON b, JSON c, JSON d) => JSON ((String, a), (String, b), (String, c), (String, d)) where
  toJSON ((k1, v1), (k2, v2), (k3, v3), (k4, v4)) =
    JObj [(k1, toJSON v1), (k2, toJSON v2), (k3, toJSON v3), (k4, toJSON v4)]

instance (JSON a, JSON b, JSON c, JSON d, JSON e) => JSON ((String, a), (String, b), (String, c), (String, d), (String, e)) where
  toJSON ((k1, v1), (k2, v2), (k3, v3), (k4, v4), (k5, v5)) =
    JObj [(k1, toJSON v1), (k2, toJSON v2), (k3, toJSON v3), (k4, toJSON v4), (k5, toJSON v5)]

```

Now, we can simply write

```
hs = ("name"    , "Ranjit")
     ,("age"    , 41.0)
     ,("likes"  , ["guacamole", "coffee", "bacon"])
     ,("hates"  , ["waiting", "grapefruit"])
     ,("lunches", lunches)
     )
```

which is a Haskell value that describes our running JSON example, and can convert it directly like so

```
js2 = toJSON hs
```

Serializing Environments

To wrap everything up, lets write a routine to serialize our `Env`

```
instance JSON (Env k v) where
  toJSON env = ???
```

and presto! our serializer *just works*

```
λ> env0  
Bind "cat" 10.0 (Bind "dog" 20.0 (Def 0))
```

```
λ> toJSON env0  
JObj [ ("cat", JNum 10.0)  
      , ("dog", JNum 20.0)  
      , ("def", JNum 0.0)  
      ]
```

Thats it for today.

We will see much more typeclass awesomeness in the next few lectures...

(<https://ucsd-cse130.github.io/sp19/feed.xml>) (<https://twitter.com/ranjitjhala>)
(<https://plus.google.com/u/0/104385825850161331469>) (<https://github.com/ranjitjhala>)

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